

Assigned	Assignment (Check due dates and time assignments are due in mathXL)
Mon. 8/12/2024 Tues. 8/13/2024	Introduction assignment in MathXL: Go to <a href="http://washoeschools.net">washoeschools.net</a> , click on <b>Students and Parents</b> then scroll down to <b>envision Mathematics</b> <b>*Syllabus Signed *Pay \$3 Lab Fee to Bookkeeper 1.1 Day 1</b>
Wed. 8/14/2024 Thur. 8/15/2024	1.1 Worksheet: Fractions (finish → Day 2)
Fri. 8/16/2024 Mon. 8/19/2024	1.2 MathXL: Order of Operation Intro MathXL
Tues. 8/20/2024 Wed. 8/21/2024	1.3 MathXL: Variables, Expressions, and Equations
Thur. 8/22/2024 Fri. 8/23/2024	1.4 MathXL: Real Numbers on the Number Line, Absolute Value
Mon. 8/26/2024 Tues. 8/27/2024	1.5 MathXL: Add and Subtract with Signed Numbers
Wed. 8/28/2024 Thur. 8/29/2024	1.6 MathXL: Multiply and Divide with Signed Numbers
Fri. 8/30/2024 Mon. 9/2/2024	Ch 1 Practice Test
Tues. 9/3/2024 Wed. 9/4/2024	Ch 1 Test

Paper  
assg.  
Simplify  
mult.  
divide

## 1.1 Fractions

### Factors:

Parts which are multiplied

$2 \cdot 5 = 10$  product  
↑ ↑  
factors

### Product:

Answer to a multiplication problem

### Prime Number:

A number only divisible by itself and 1

$$13 = 13 \cdot 1$$

No other factors

### Composite number:

A number made up of multiple factors.

$$12 = 3 \cdot 4$$

$$12 = 3 \cdot 2 \cdot 2$$

Not prime

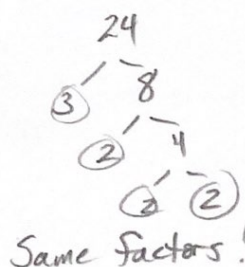
### Factoring Numbers

Write each number as the product of prime factors.

(a) 35  $35 = 5 \cdot 7$

(b) 24  $24 = 4 \cdot 6$   
 $24 = 2 \cdot 2 \cdot 2 \cdot 3$

### Factor Trees



**Vocabulary:**Fraction:Ex.  $\frac{2}{5}$  part  
wholeMixed number:

$$2\frac{1}{3} = 2 + \frac{1}{3}$$

Proper fraction:

top is small



$$\frac{2}{3}$$

Improper fraction:

top is large

$$\frac{5}{3} = 2\frac{2}{3}$$

Numerator:

top #

Denominator:

bottom #

Reciprocals:

one is flipped

$$\frac{2}{7} \text{ \& } \frac{7}{2} \quad \left\{ \begin{array}{l} 3 \text{ \& } \frac{1}{3} \\ \frac{3}{7} \text{ \& } \frac{7}{3} \end{array} \right.$$

Zero vs Undefined!

$$\frac{0}{4} = 0$$

$$\frac{4}{0} \text{ is undef.}$$

Writing Fractions in Lowest TermsSimplify each fraction / Write each in lowest terms:

$$\text{a) } \frac{12 \div 3}{15 \div 3} = \frac{4}{5} \quad \text{OR} \quad \frac{12}{15} = \frac{\cancel{3} \cdot 4}{\cancel{3} \cdot 5} = \frac{4}{5}$$

$$\text{b) } \frac{15 \div 5}{45 \div 5} = \frac{3 \div 3}{9 \div 3} = \frac{1}{3} \quad \text{OR} \quad \frac{15}{45} = \frac{5 \cdot \cancel{3}}{5 \cdot \cancel{3} \cdot 3} = \frac{1}{3}$$

Multiplying Fractions

Find each product and write it in lowest terms:

$$\text{a) } \frac{3}{8} \cdot \frac{4}{9} = \frac{3 \cdot 4}{8 \cdot 9} = \frac{12}{72} \div 12 = \frac{1}{6}$$

$$\text{OR } \frac{\cancel{3}}{\cancel{4} \cdot 2} \cdot \frac{\cancel{4}}{\cancel{3} \cdot 3} = \frac{1}{6}$$

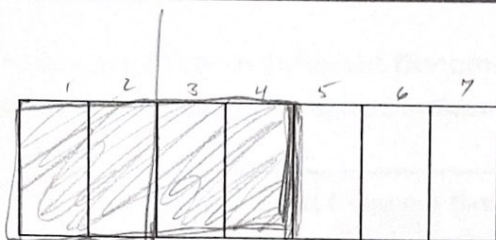
$$\text{b) } \frac{4}{7} \cdot \frac{5}{12} = \frac{20}{84} \div 4 = \frac{5}{21}$$

$$\text{OR } \frac{\cancel{4}}{7} \cdot \frac{5}{\cancel{4} \cdot 3} = \frac{5}{21}$$

To multiply fractions, multiply numerators and multiply denominators. (Go straight across!)

Another option is to break the numbers into FACTORS, then CANCEL any factor that is in the numerator and denominator.



**Consider this:**What is half of  $\frac{4}{7}$ ?Half is  $\frac{2}{7}$ 

$$\Rightarrow \frac{1}{2} \cdot \frac{4}{7} = \frac{4}{14} = \boxed{\frac{2}{7}}$$

What is  $\frac{4}{7}$  divided by 2? Same as half!So,  $\frac{4}{7} \div \frac{2}{1}$  is the same thing as  $\frac{4}{7} \cdot \frac{1}{2}$ !

To divide fractions, rewrite the problem as multiplying by the reciprocal.

- Keep the first fraction
- Flip the second fraction
- Multiply!

**Dividing Fractions**

Find each quotient and write it in lowest terms.

a)  $\frac{3}{4} \div \frac{8}{5}$

$$= \frac{3}{4} \cdot \frac{5}{8}$$

$$= \boxed{\frac{15}{32}}$$

b)  $\frac{5}{6} \div \frac{30}{1}$

$$= \frac{5}{6} \cdot \frac{1}{30}$$

$$= \frac{5}{6} \cdot \frac{1}{5 \cdot 6}$$

$$= \boxed{\frac{1}{36}}$$

c)  $\frac{2}{7} \div \frac{8}{9}$

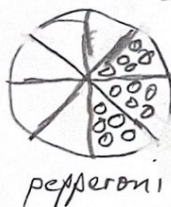
$$= \frac{2}{7} \cdot \frac{9}{8}$$

$$= \frac{2}{7} \cdot \frac{9}{2 \cdot 4}$$

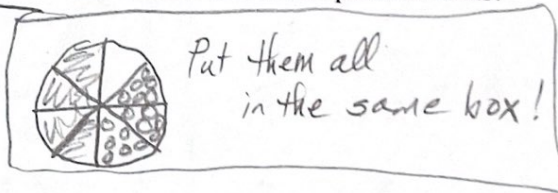
$$= \boxed{\frac{9}{28}}$$

**Now consider this one:**

Your take-out pizzas are cut in 8 slices. Everyone eats what they want and you are putting leftovers away. There are 3 slices left of pepperoni and 4 slices left of cheese pizza. What fraction of a whole pizza remains?



$$\frac{3}{8} + \frac{4}{8} = \boxed{\frac{7}{8}}$$



Adding Fractions with the Same Denominator

Find each sum, and write it in lowest terms.

(a)  $\frac{3}{7} + \frac{2}{7} = \boxed{\frac{5}{7}}$

(b)  $\frac{2}{10} + \frac{3}{10} = \frac{5}{10} \div 5 = \boxed{\frac{1}{2}}$

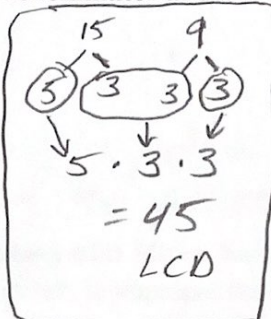
**To add fractions with the same denominator:**

- Keep the denominator (treat it as the "size" of the pieces)
- Add the numerators (how many pieces total of that size)

## Adding Fractions with Different Denominators

Find a common denominator and build one or more fractions bigger so that you can add them:

$$\begin{aligned} \text{(a)} \quad & \frac{4}{15} + \frac{5}{9} \\ & \frac{4 \cdot 3}{15 \cdot 3} + \frac{5 \cdot 5}{9 \cdot 5} \\ & = \frac{12}{45} + \frac{25}{45} \\ & = \boxed{\frac{37}{45}} \end{aligned}$$

**Least Common Denominator (LCD):**

smallest big thing they both go into

Steps:

- 1) Find the LCD. *Need factors from each! Use common factors ONCE*
- 2) Multiply numerator & denominator by the same thing to build one (or more) fraction(s) bigger so you have the same denominator in all fractions.
- 3) Keep the denominator and add the numerators.
- 4) Write your answer in lowest terms. (Simplify)

$$\text{c)} \quad \frac{3}{7} + \frac{1}{14}$$

Do this one 1st!

$$= \frac{3 \cdot 2}{7 \cdot 2} + \frac{1}{14}$$

$$= \frac{6}{14} + \frac{1}{14} = \frac{7}{14} \div 7 = \boxed{\frac{1}{2}}$$

## Subtracting Fractions

Find each difference, and write it in lowest terms.

$$\text{(a)} \quad \frac{15}{8} - \frac{3}{8} = \frac{12}{8}$$

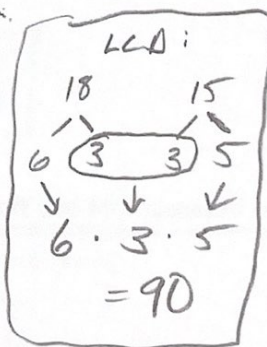
$$\frac{12 \div 4}{8 \div 4} = \boxed{\frac{3}{2}}$$

$$\text{(b)} \quad \frac{7}{18} - \frac{4}{15}$$

$$\frac{7 \cdot 5}{18 \cdot 5} - \frac{4 \cdot 6}{15 \cdot 6}$$

$$= \frac{35}{90} - \frac{24}{90}$$

$$= \boxed{\frac{11}{90}}$$



$$\text{c)} \quad \frac{7}{9} - \frac{1}{3} + \frac{1}{9}$$

$$\frac{7}{9} - \frac{1 \cdot 3}{3 \cdot 3} + \frac{1}{9}$$

$$= \frac{7}{9} - \frac{3}{9} + \frac{1}{9}$$

$$= \frac{7-3+1}{9}$$

$$= \boxed{\frac{5}{9}}$$



**One last thing to consider:**

Your take-out pizzas are cut in 8 slices. You are gathering up leftovers after dinner.

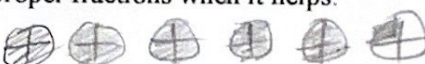
There are 5 slices left of pepperoni, and 6 slices left of cheese pizza. What fraction of a whole pizza remains?

$$\frac{5}{8} + \frac{6}{8} = \boxed{\frac{11}{8}} \Rightarrow 11 \div 8 = 1R3 \text{ or } 1\frac{3}{8}$$

Try drawing a picture and putting the pieces back in 1 box. See how many don't fit!

**Example 8: Working with Mixed Numbers**

Change mixed numbers to improper fractions when it helps:

(a)  $5\frac{1}{4} = 5 \text{ whole} + \frac{1}{4} =$    $= \frac{4}{4} + \frac{4}{4} + \frac{4}{4} + \frac{4}{4} + \frac{4}{4} + \frac{1}{4} = \frac{4+4+4+4+4+1}{4} = \boxed{\frac{21}{4}}$

$5\frac{1}{4} \rightarrow \frac{21}{4}$   
 5  $\cdot$  4 (5 groups of 4)  
 + 1 more  $\rightarrow$  21

(b)  $3\frac{1}{2} + 2\frac{3}{4} \rightarrow \frac{7}{2} + \frac{11}{4}$   
 $\frac{7 \cdot 2}{2 \cdot 2} + \frac{11}{4} = \frac{14}{4} + \frac{11}{4} = \boxed{\frac{25}{4}}$

(c)  $2\frac{1}{3} \cdot 5\frac{1}{4}$   
 $\frac{7}{3} \cdot \frac{21}{4} = \frac{7}{\cancel{3}} \cdot \frac{\cancel{3} \cdot 7}{4} = \boxed{\frac{49}{4}}$

(d)  $3\frac{3}{4} \div 4\frac{2}{5}$

$$\frac{15}{4} \div \frac{22}{5} = \frac{15}{4} \cdot \frac{5}{22} = \boxed{\frac{75}{88}}$$

$$\begin{array}{r} 35 \\ 5 \\ \hline 75 \end{array}$$

(e) A board is  $10\frac{1}{2}$  feet long. If it must be sectioned off into four pieces of equal length for shelves, how long must each piece be?

division

$$10\frac{1}{2} \div 4$$

$$\frac{21}{2} \div 4$$

$$\frac{21}{2} \cdot \frac{1}{4} = \boxed{\frac{21}{8}}$$

$$21 \div 8 = \boxed{2\frac{5}{8}} \text{ feet}$$

$$\begin{array}{r} 2\frac{5}{8} \\ 8 \overline{)21} \\ \underline{-16} \\ 5 \end{array}$$