Algebra 2 Worksheet 5.1

Find the solutions to f(x) = 0.

1.
$$f(x) = 4(x+1)(x-5)$$
 2. $f(x) = 2x^2 + 10x$

$$2. \ f(x) = 2x^2 + 10x$$

3.
$$f(x) = (2x + 1)(3x - 5)$$

4.
$$f(x) = 2.1(x - 2.34)(x + 1)$$
 5. $f(x) = 3(5x + 6)(x - 7)$

5.
$$f(x) = 3(5x + 6)(x - 7)$$

6.
$$y = x^2 + 6x$$

7.
$$f(x) = 3x^2 + 27x$$
 8. $y = 27x^2 + 3x$

8.
$$y = 27x^2 + 3x$$

9.
$$f(x) = 5x^2 + 6x$$

10.
$$2x + 3 = y$$

11.
$$20x = 5x^2$$

12.
$$f(x) = 2(x+1)^2 - 12$$
 13. $y = x^2 - 8x - 20$ 14. $-3x^2 + 14 = 2$

13.
$$v = x^2 - 8x - 20$$

$$14. -3x^2 + 14 = 2$$

15.
$$x^2 - x = 42$$

$$16. -4x^2 + 37 = 1$$

16.
$$-4x^2 + 37 = 1$$
 17. $y = x^2 - 6.21x$

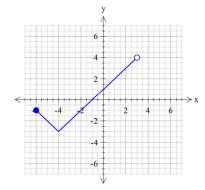
18.
$$x^2 + 13x + 10 = -32$$
 19. $(x - 5)^2 + 84 = 20$ 20. $x^2 = -7x - 12$

19.
$$(x-5)^2 + 84 = 20$$

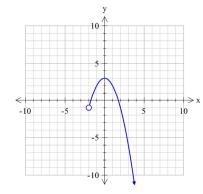
$$20. \ x^2 = -7x - 12$$

Describe the domain and range of the following functions in interval notation.

21.



22.



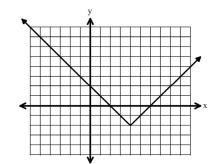
- 23. Given f(x) = 3(x 4) + 1, identify the name of the parent function and describe how the graph is transformed from the parent function.
 - A. Quadratic Function with a vertical compression, translated right 4 and up 1
 - B. Quadratic Function with a vertical stretch, translated right 4 and up 1
 - C. Linear Function with a vertical compression, translated left 4 and up 1
 - D. Linear Function with a vertical stretch, translated right 4 and up 1
- 24. Which equation is obtained after the translation of the graph up 2 units and left 6 units?

A.
$$f(x) = |x - 2|$$

B.
$$f(x) = |x| - 2$$

C.
$$f(x) = |x + 2|$$

D.
$$f(x) = |x| + 2$$



25. Solve for y: 4 + yx + 2y = 3x + 4

Algebra 2 Worksheet 5.2

Find the solutions to f(x) = 0.

$$1. f(x) = x(x+3)(x-7)$$

2.
$$f(x) = -2(x+3)^2 + 32$$

1.
$$f(x) = x(x+3)(x-7)$$
 2. $f(x) = -2(x+3)^2 + 32$ 3. $y = (3x+2)(4x-5)(x+4)$

4.
$$f(x) = x^3 + 3x^2 - 10x$$
 5. $y = -x^2 - 6x + 40$ 6. $f(x) = x^3 + 2x^2 - 8x$

5.
$$y = -x^2 - 6x + 40$$

6.
$$f(x) = x^3 + 2x^2 - 8x$$

7.
$$x^3 + 10x^2 + 29x = 4x$$
 8. $2x^3 + 10x^2 = -8x$ 10. $50x^4 = -5x^3$

8.
$$2x^3 + 10x^2 = -8x$$

10.
$$50x^4 = -5x^3$$

11.
$$(x+3)^2 + 85 = 4$$
 12. $4x^2 - 3x^3 = 0$ 13. $-3x^2 + 15x = 0$

12.
$$4x^2 - 3x^3 = 0$$

$$13. \ -3x^2 + 15x = 0$$

14. Which of the following could be the equation for g(x)?

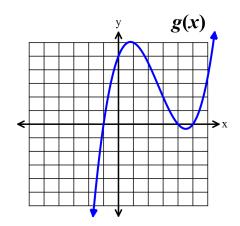
A.
$$f(x) = 3(x-1)(x+4)(x+5)$$

B.
$$f(x) = \frac{1}{4}(x+1)(x-4)(x-5)$$

C.
$$f(x) = -x(x-1)(x+4)(x+5)$$

D.
$$f(x) = x(x+1)(x-4)(x-5)$$

15. What is the range of the function g(x) from #14?



16. Do
$$f(x)$$
 and $g(x)$ cross the x-axis in the same places?

$$\begin{cases} f(x) = -x^2(x+15)(x-6) \\ g(x) = 5x(x+15)(x-6) \end{cases}$$

17. The graph of $f(x) = x^2$ is vertically compressed by a factor of $\frac{1}{2}$ and translated to the right three units and down one unit to produce the function g(x). Which of the following equations represents g(x)?

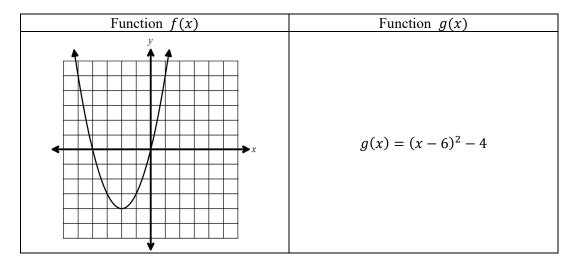
A.
$$g(x) = -\frac{1}{2}(x+3)^2 + 1$$

C.
$$g(x) = \frac{1}{2}(x-3)^2 - 1$$

B.
$$g(x) = -\frac{1}{2}(x+1)^2 + 3$$

D.
$$g(x) = \frac{1}{2}(x-1)^2 - 3$$

18. Compare the two functions represented below. Determine which of the following statements is true.



- A. The functions have the same vertex.
- B. The minimum value of f(x) is the same as the minimum value of g(x).
- C. The functions have the same axis of symmetry.
- D. The minimum value of f(x) is less than the minimum value of g(x).

Simplify.

19.
$$(2+3i)^2$$

20.
$$(3 - \sqrt{5})(3 + \sqrt{5})$$

21.
$$5i(6-11i)$$

Algebra 2 Worksheet 5.3

Find the solutions to f(x) = 0.

1.
$$f(x) = 3x^2 - 7x - 6$$

2.
$$f(x) = x^4 - 10x^2 + 9$$

3.
$$x^2 - 85 = -4$$

4.
$$32x^2 - 18 = f(x)$$

5.
$$2x^2 + 2x = 12$$

6.
$$y = x^4 - 2x^2 + 1$$

7.
$$f(x) = 9x^4 - 16x^2$$

8.
$$y = -x^6 + 36x^4$$

9.
$$x^2 - 2x - 14 = -5x + 4$$

10.
$$6x^2 - 5x = 4$$

11.
$$-10x^2 - 6x + 4 = 0$$

12.
$$-3x^3 + 243x = 0$$

13.
$$3x^2 + 18x = f(x)$$

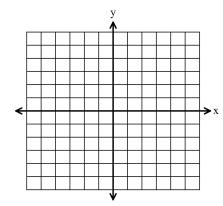
14.
$$x^4 - 81 = 0$$

15.
$$\begin{cases} f(x) = -(x-1)(x-5) \\ g(x) = x^2 - 6x + 13 \end{cases}$$

- a.) Do f(x) and g(x) have the same vertex?
- b.) Do f(x) and g(x) have the same axis of symmetry?
- c.) Do f(x) and g(x) have the same range?

16. Graph the piecewise function.

$$f(x) = \begin{cases} -3 & x < -2 \\ -x + 1 & -2 \le x < 3 \\ |x - 5| & x \ge 3 \end{cases}$$



Solve each of the following quadratics using the quadratic formula. Simplify all answers, using i if needed.

1.)
$$x^2 - 4x - 5 = 0$$

2.)
$$x^2 - 8x + 1 = 0$$

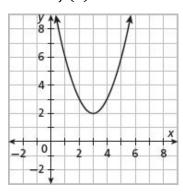
3.)
$$x^2 + 8x + 19 = 0$$

4.)
$$-3r^2 = 6r - 10$$

$$5.) \quad 3 - 8v - 5v^2 = 2v$$

6.)
$$-4x^2 + 2x = 5$$

7.) The function f(x) is graphed below. What are the solutions to f(x) = 0?



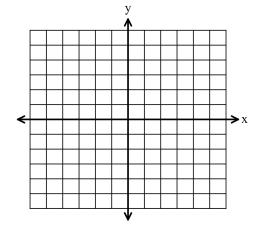
8.) Graph $f(x) = x^2 - 8x + 15$ and give the following information: Hint: probably easiest to convert the equation to $y = a(x - h)^2 + k$ form

Vertex:

Min/Max:

y-intercept:

x-intercepts:



9.) The graph of $g(x) = -x^2 + 10x - 9$ models the height of one of the arches of a doorway, in feet. How wide is the doorway?

10.) What is the height of the doorway at the highest point?

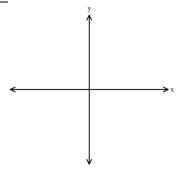
11.) The quadratic equation $y = x^2 - 10x + 21$ is shifted left 6 units and down 8 units. What is the new equation, written in vertex form?

Algebra 2 Worksheet 5.5

1. Use a graphing calculator to solve

the following system:
$$\begin{cases} f(x) = -x^2 + 4x + 11 \\ g(x) = 3x + 4 \end{cases}$$

2. Draw a sketch:



3.
$$\begin{cases} f(x) = 3x^2 - 9x + 3 \\ g(x) = 6x + 3 \end{cases}$$

4.
$$\begin{cases} x^2 + 4x - 3y = 6 \\ -x + y = 2 \end{cases}$$

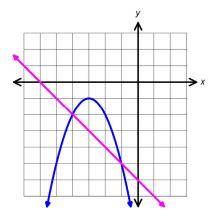
5.
$$\begin{cases} f(x) = -2x^2 + 4x + 1 \\ g(x) = -x + 3 \end{cases}$$

6.
$$\begin{cases} x^2 + 6x - 8 = y \\ y = 4x + 7 \end{cases}$$

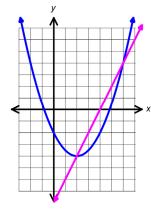
7.
$$\begin{cases} 6x^2 + 27x - 3y = 108 \\ 5x - y = 6 \end{cases}$$

8. In the xy-plane, the parabola with equation $y = (x - 11)^2$ intersects the line with equation y = 25 at two points, A and B. What is the length of \overline{AB} ?

9. Solve the system:



10. Solve the system:



11. Use the system of equations below. Which statement best describes the solution set of the system?

$$\begin{cases} x = 4 \\ y = 2 \end{cases}$$

- A. The solution set is only the ordered pair (4, 2).
- B. The solution set is all ordered pairs where x = 4; y can be any real number.
- C. The solution set is all ordered pairs where y = 2; x can be any real number.
- D. There is no solution to the system.
- 12.

Which of the following systems of equations could a student use to write a quadratic function in standard form for the parabola passing through the points (1, 4), (3, -2), and (-2, 17)?

A.
$$\begin{cases} a + 4b + c = y \\ 9a - 2b + c = y \\ -4a + 17b + c = y \end{cases}$$

C.
$$\begin{cases} 2a+b+c=4\\ 6a+3b+c=-2\\ -4a-2b+c=17 \end{cases}$$

B.
$$\begin{cases} a+b+c=4\\ 9a+3b+c=-2\\ 4a-2b+c=17 \end{cases}$$

$$\mathbf{D.} \begin{cases} x^2 + 4x + c = y \\ 3x^2 - 2x + c = y \\ -2x^2 + 17x + c = y \end{cases}$$

13.) What are the solutions to the quadratic equation, $y^2 + 2y = 9 + 5y$?

A.
$$y = \frac{3 \pm 3i\sqrt{3}}{2}$$

$$C. \quad y = \frac{3 \pm 3i\sqrt{5}}{2}$$

B.
$$y = \frac{-3 \pm 3\sqrt{5}}{2}$$

D.
$$y = \frac{3 \pm 3\sqrt{5}}{2}$$

#1-16: Find the solutions, or zeroes or roots, to each function or equation by using the best method (square rooting, factoring, or the quadratic formula). Simplify all answers using t if needed.

1.)
$$\frac{1}{2}x^2 + 5 = 41$$
 2.) $x^2 + 6x - 27 = 0$

$$2.) \quad x^2 + 6x - 27 = 0$$

$$3.) \ x^2 + 5x - 99 = 3x$$

4.)
$$-4x^2 + 18x - 4 = 10x$$
 5.) $2(x-6)^2 - 45 = 53$

5.)
$$2(x-6)^2 - 45 = 53$$

6.)
$$f(x) = 2x^2 - 4x - 1$$

7.)
$$-4x^2 + 25 = 0$$

8.)
$$-3(x+4)^2 - 18 = 6$$

9.)
$$y = 2x^3 - 9x^2 + 4x$$

10.)
$$3x^2 + 5x - 3 = 4x - 8$$

11.)
$$-3x^2 + 50 = 2$$

12.)
$$x^4 - 50x^2 + 54 = 5$$

13.)
$$16x^2 - 14x = 0$$

14.)
$$3x^2 + 4x + 12 = 15$$

15.)
$$x^2 + 8x + 6 = 3x$$

$$16.) -2x^3 + 16x = 0$$

17.) The graph of $h(x) = -x^2 + 10x - 16$ models the height, in feet, of one of the arches at the entrance of a parking structure. What is the width of the parking structure at the base?

18.) Which of following functions does NOT represent the parabola with a vertex at (1, 4) and x-intercepts (-1, 0) and (3, 0).

A.
$$f(x) = -x^2 + x + 4$$

C.
$$f(x) = -x^2 + 2x + 3$$

B.
$$f(x) = -(x-1)^2 + 4$$

D.
$$f(x) = -(x+1)(x-3)$$

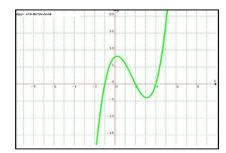
19.) Compare the axis of symmetry and the minimum values for the two functions below.

$$h(x) = 2(x+3)(x-7)$$

$$j(x) = x^2 - 4x - 21$$

Determine which of the following statements is correct.

- A. The functions h(x) and j(x) have the same axis of symmetry, but the minimum value of h(x) is less than the minimum value of j(x).
- B. The functions h(x) and j(x) have the same axis of symmetry, but the minimum value of h(x) is greater than the minimum value of j(x).
- C. The functions h(x) and j(x) do not have the same axis of symmetry, and the minimum value of h(x) is less than the minimum value of j(x).
- D. The functions h(x) and j(x) do not have the same axis of symmetry, and the minimum value of h(x) is greater than the minimum value of j(x).
- 20) Write a possible equation for the function graphed below:



Find the solutions for f(x) = 0 in the following functions:

$$21.) \quad f(x) = -13x^4 + 39x^3$$

22.)
$$f(x) = 4x^2 - 4x - 3$$

For 23-25, find the zeroes.

23.)
$$-x^{13} + 49x^{11} = 0$$

24.)
$$x^2 - 50 = 14$$

25.)
$$2x^3 - 50x = 0$$

Solve each system algebraically:

26.)
$$\begin{cases} f(x) = 2x^2 + 8x - 7 \\ g(x) = -4x - 7 \end{cases}$$

27.)
$$\begin{cases} f(x) = 2x^2 - 6x + 7 \\ g(x) = 5x - 5 \end{cases}$$

28.)
$$\begin{cases} x^2 + 8x + 10y + 7 = 19\\ 3x + 5y = 2 \end{cases}$$

29) Which of the following systems of equations could a student use to write a quadratic function in standard form for the parabola passing through the points (-3, -4), (6, 5) and (-1, 12)?

A.
$$\begin{cases} 9a - 3b + c = -4 \\ 36a + 6b + c = 5 \\ a - b + c = 12 \end{cases}$$

C.
$$\begin{cases} 9a - 4b + c = y \\ 36a + 5b + c = y \\ a + 12b + c = y \end{cases}$$

B.
$$\begin{cases} -6a - 3b + c = -4 \\ 12a + 6b + c = 5 \\ -2a - b + c = 12 \end{cases}$$

D.
$$\begin{cases} -3x^2 - 4x + c = y \\ 6x^2 + 5x + c = y \\ -x^2 + 12b + c = y \end{cases}$$