

2.2 Examples

1) Given the following conditional statement: If you live in Chicago, then you live in Illinois.

- a) Write the converse.

- b) Write the inverse.

- c) Write the contrapositive.

- d) Which of the statements are true?

- e) Write the biconditional for this conditional. Is it a true statement? Explain.

2) If two lines in the same plane do not intersect, then they are parallel lines.

- a) Write the contrapositive.

- b) Write the converse.

- c) Write the inverse.

- d) Which of the statements are true?

- e) Write the biconditional for this conditional. Is it a true statement? Explain.

A postulate or axiom is a statement that is accepted as true without proof.

Postulates about points, lines, and planes:

- Through any two points there is exactly one line.
- Through any three noncollinear points, there is exactly one plane.
- A line contains at least 2 points.
- A plane contains at least 3 noncollinear points.
- If two points lie in a plane, then the entire line containing those points lies in the plane.
- If 2 lines intersect, then their intersection is exactly one point.
- If 2 planes intersect, then their intersection is a line.
- If 3 planes intersect, then their intersection is a point.

A theorem is a statement or conjecture that has been proven.

Theorem: If a point is a midpoint, then it divides a segment into 2 congruent segments.

Look at your proof packet for 2.4 examples on 2-column proofs.

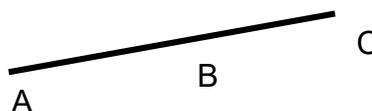
Other examples: Are the following statements Sometimes, Always, or Never true?

1) Points X and Y are in plane z. Any point collinear with X and Y is in plane z.

2) Two planes have an intersection of a line.

Paragraph Proof: It is acceptable to write a paragraph of a proof, rather than using two columns.

Example: Write a paragraph proof. If $AB = 6$ and $BC = 6$, then prove that B is the midpoint of AC.



Inductive versus Deductive Reasoning:

Law of Detachment:

Law of Syllogism

Example 1: Draw a conclusion. Which type of reasoning is used?

If Eduardo goes to a concert tonight, he will miss football practice. Tonight, Eduardo went to a concert.

Conclusion:

Example 2: Is the conclusion valid or invalid? If it is valid, what type of reasoning is used?

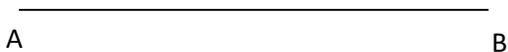
If two angles form a linear pair, then they are supplementary. If two angles are supplementary, then they have a sum of 180. **Conclusion:** If two angles form a linear pair, then they have a sum of 180.

Example 2: Is the conclusion valid or invalid? If it is valid, what type of reasoning is used?

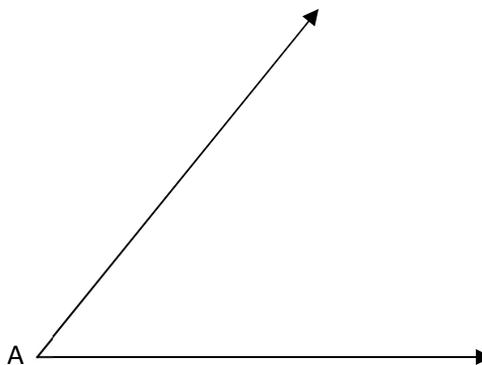
If two angles form a linear pair, then they are supplementary. If two angles are supplementary, then they have a sum of 180. **Conclusion:** If two angles have a sum of 180, then they are a linear pair.

Constructions:

1. Construct the bisector of \overline{AB} (p.28)



2. Construct the bisector of $\angle A$ (p.40)



3. Copy \overline{AB} from #1 (p.16)



4. Copy $\angle A$ from #2 on line ℓ (p. 39)



2.6 Guided Notes

For the following postulates, you may use their names in proofs.

Angle Addition Postulate: If D is in the interior of $\angle ABC$, then $m\angle ABD + m\angle DBC = m\angle ABC$.

For all of the theorems below, you must write out the entire theorem in words or symbols.

- If two angles form a linear pair, then they are supplementary angles.

- If two adjacent angles form a right angle, then they are complementary angles.

- If angles are supplementary to the same angle (or to congruent angles), then they are congruent.

- If angles are complementary to the same angle (or to congruent angles), then they are congruent.

- If two angles are vertical, then they are congruent.

- If two lines are perpendicular, then they form four right angles.
- If two angles are right angles, then they are congruent.
- If two lines are perpendicular, then they form congruent adjacent angles.

Complete the proofs from the Ch 2 Proofs Packet.

Solving examples:

1) The complement of the supplement of $\angle A$ is 37° . Find the measure of $\angle A$.

2) $\angle A$ is complementary to $\angle B$, and $\angle C$ is complementary to $\angle A$. If $\angle B = (3x + 10)$ and $\angle C = (5x - 2)$, then find the measure of $\angle A$.